

(14) Find  $\lim_{n \rightarrow \infty} \frac{n! \cos n}{(n+1)!}$ .

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$$= \lim_{n \rightarrow \infty} \frac{n! \cos n}{n! (n+1)}$$

Squeeze Theorem:

$$0 = \lim_{n \rightarrow \infty} \frac{-1}{n+1} \leq \lim_{n \rightarrow \infty} \frac{\cos n}{n+1} \leq \lim_{n \rightarrow \infty} \frac{1}{n+1} = 0$$

Thus  $\lim_{n \rightarrow \infty} \frac{\cos n}{n+1} = \boxed{0}$ .

(15) Find  $\lim_{n \rightarrow \infty} \frac{(3+n)^n}{n^n}$ .

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$$= \lim_{n \rightarrow \infty} \left( \frac{3}{n} + 1 \right)^n$$

$$= \lim_{n \rightarrow \infty} \left( 1 + \frac{(3)}{n} \right)^n$$

$$= \boxed{e^3} \quad \left( \text{since } e^x = \lim_{n \rightarrow \infty} \left( 1 + \frac{x}{n} \right)^n \right)$$

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(16) Describe the boundedness & monotonicity of  $\left\langle \frac{1}{4}, -\frac{1}{6}, \frac{1}{8}, -\frac{1}{10}, \frac{1}{12}, \dots \right\rangle$ .

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The sequence is bounded since all terms are between  $\pm 1$ .

The sequence is not monotonic since it decreases from  $\frac{1}{4}$  to  $-\frac{1}{6}$  and increases from  $-\frac{1}{6}$  to  $\frac{1}{8}$ .

The Monotonic sequence theorem doesn't apply, but it still appears to converge to 0.